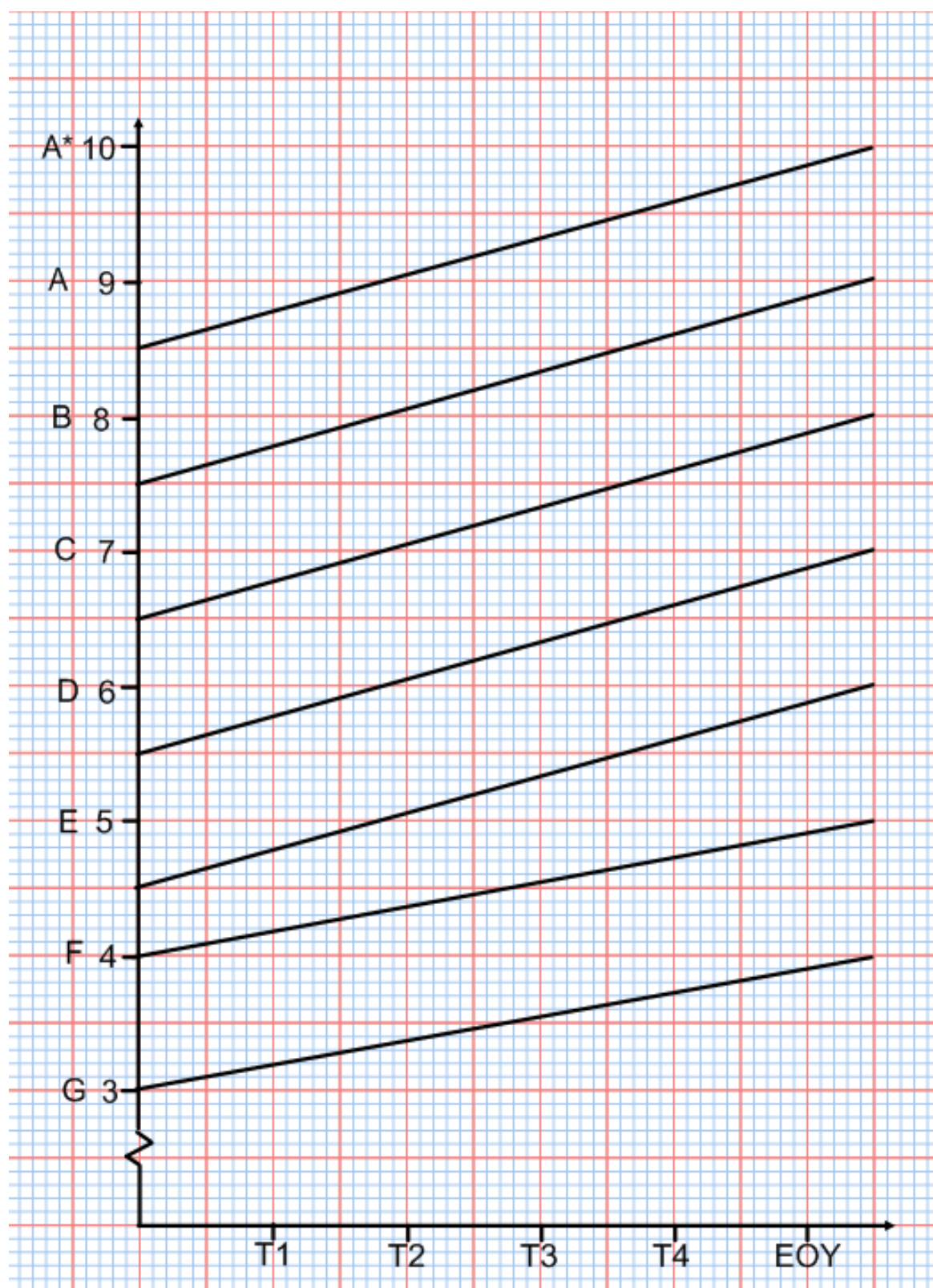


Mathematics GCSE  
Higher  
Student Booklet Year 10

Name..... Form.....



## Year 10 Progress chart



After each test you must plot your level on the graph and then set your targets.

| TEST | TARGETS |
|------|---------|
| 1    |         |
| 2    |         |
| 3    |         |
| 4    |         |
| EOY  |         |

# Term 1 Objectives

| Module 1: Integers                                                                                             | Notes | 😊 | 😐 | 😞 |
|----------------------------------------------------------------------------------------------------------------|-------|---|---|---|
| Use brackets and the hierarchy of operations (BIDMAS)                                                          |       |   |   |   |
| Add, subtract, multiply and divide integers, negative numbers and decimals                                     |       |   |   |   |
| Round decimals to appropriate numbers of decimal places or significant figures                                 |       |   |   |   |
| Multiply and divide by any number between 0 and 1                                                              |       |   |   |   |
| Check their calculations by rounding, eg $29 \times 31 \approx 30 \times 30$                                   |       |   |   |   |
| Multiply and divide decimal numbers by whole numbers and decimal numbers (up to 2 d.p.), eg $266.22 \div 0.34$ |       |   |   |   |
| Equivalent Calculations:<br>Know that, eg $13.5 \div 0.5 = 135 \div 5$                                         |       |   |   |   |

| Module 2: Coordinates                                                                        | Notes | 😊 | 😐 | 😞 |
|----------------------------------------------------------------------------------------------|-------|---|---|---|
| Use axes and coordinates to specify points in all four quadrants in 2-D and 3-D              |       |   |   |   |
| Identify points with given coordinates                                                       |       |   |   |   |
| Identify coordinates of given points                                                         |       |   |   |   |
| Find the coordinates of points identified by geometrical information in 2-D and 3-D          |       |   |   |   |
| Find the coordinates of the midpoint of a line segment, AB, given the coordinates of A and B |       |   |   |   |

| Module 3: Fractions                                   | Notes | 😊 | 😐 | 😞 |
|-------------------------------------------------------|-------|---|---|---|
| Find equivalent fractions                             |       |   |   |   |
| Find fractions of an amount                           |       |   |   |   |
| Add, subtract, multiply and divide fractions          |       |   |   |   |
| Multiply and divide fractions including mixed numbers |       |   |   |   |

| Module 4: Algebra                                                                 | Notes | 😊 | 😐 | 😞 |
|-----------------------------------------------------------------------------------|-------|---|---|---|
| Use notation and symbols correctly                                                |       |   |   |   |
| Write an expression                                                               |       |   |   |   |
| Select an expression/identity/equation/formula from a list                        |       |   |   |   |
| Manipulate algebraic expressions by collecting like terms                         |       |   |   |   |
| Multiply a single term over a bracket                                             |       |   |   |   |
| Factorise algebraic expressions by taking out common factors                      |       |   |   |   |
| Expand the product of two linear expressions                                      |       |   |   |   |
| Factorise quadratic expressions including using the difference of two squares     |       |   |   |   |
| Simplify rational expressions by cancelling, adding, subtracting, and multiplying |       |   |   |   |

END OF HALF TERM: Test 1

| Module 5: Shapes & Angles                                                                                                     | Notes | 😊 | 😐 | 😞 |
|-------------------------------------------------------------------------------------------------------------------------------|-------|---|---|---|
| Understand and use the angle properties of parallel lines                                                                     |       |   |   |   |
| Understand, draw and measure bearings                                                                                         |       |   |   |   |
| Calculate bearings and solve bearings problems                                                                                |       |   |   |   |
| Mark parallel lines on a diagram                                                                                              |       |   |   |   |
| Use the properties of corresponding and alternate angles                                                                      |       |   |   |   |
| Recognise and classify quadrilaterals                                                                                         |       |   |   |   |
| Understand and use the angle properties of quadrilaterals                                                                     |       |   |   |   |
| Explain why the angle sum of a quadrilateral is $360^\circ$                                                                   |       |   |   |   |
| Understand the proof that the angle sum of a triangle is $180^\circ$                                                          |       |   |   |   |
| Understand a proof that the exterior angle of a triangle is equal to the sum of the interior angles of the other two vertices |       |   |   |   |
| Use the size/angle properties of isosceles and equilateral triangles                                                          |       |   |   |   |
| Recall and use these properties of angles in more complex problems                                                            |       |   |   |   |
| Calculate and use the sums of the interior angles of polygons                                                                 |       |   |   |   |
| Use geometric language appropriately and recognise and name pentagons, hexagons, heptagons, octagons and decagons             |       |   |   |   |
| Use the angle sums of irregular polygons                                                                                      |       |   |   |   |

|                                                                                                                     |  |  |  |  |
|---------------------------------------------------------------------------------------------------------------------|--|--|--|--|
| Calculate and use the angles of regular polygons                                                                    |  |  |  |  |
| Use the sum of the interior angles of an n sided polygon                                                            |  |  |  |  |
| Use the sum of the exterior angles of any polygon is $360^\circ$                                                    |  |  |  |  |
| Use the sum of the interior angle and the exterior angle is $180^\circ$                                             |  |  |  |  |
| Find the size of each interior angle or the size of each exterior angle or the number of sides of a regular polygon |  |  |  |  |
| Understand tessellations of regular and irregular polygons and combinations of polygons                             |  |  |  |  |
| Explain why some shapes tessellate when other shapes do not                                                         |  |  |  |  |

| Module 6: Collecting Data                                                                                                                                                                                                                                                                                                                                | Notes | 😊 | 😐 | 😞 |
|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------|---|---|---|
| <p>Understand The Data Cycle;</p> <p>Specify the problem and plan</p> <p>Decide what data to collect and what statistical analysis is needed</p> <p>Collect data from a variety of suitable primary and secondary sources</p> <p>Use suitable data collection techniques</p> <p>Process and represent the data</p> <p>Interpret and discuss the data</p> |       |   |   |   |
| Discuss how data relates to a problem, identify possible sources of bias and plan to minimise it                                                                                                                                                                                                                                                         |       |   |   |   |
| Understand how different sample sizes may affect the reliability of conclusions drawn                                                                                                                                                                                                                                                                    |       |   |   |   |
| Identify which primary data they need to collect and in what format, including grouped data                                                                                                                                                                                                                                                              |       |   |   |   |
| Consider fairness                                                                                                                                                                                                                                                                                                                                        |       |   |   |   |
| Understand sample and population                                                                                                                                                                                                                                                                                                                         |       |   |   |   |
| Design a question for a questionnaire                                                                                                                                                                                                                                                                                                                    |       |   |   |   |
| Criticise questions for a questionnaire                                                                                                                                                                                                                                                                                                                  |       |   |   |   |
| Design an experiment or survey                                                                                                                                                                                                                                                                                                                           |       |   |   |   |
| Select and justify a sampling scheme and a method to investigate a population, including random and stratified sampling                                                                                                                                                                                                                                  |       |   |   |   |
| Use stratified sampling                                                                                                                                                                                                                                                                                                                                  |       |   |   |   |

|                                                                                 |  |  |  |  |
|---------------------------------------------------------------------------------|--|--|--|--|
| Design and use data-collection sheets for grouped, discrete and continuous data |  |  |  |  |
| Collect data using various methods                                              |  |  |  |  |
| Sort, classify and tabulate data and discrete or continuous quantitative data   |  |  |  |  |
| Group discrete and continuous data into class intervals of equal width          |  |  |  |  |
| Extract data from lists and tables                                              |  |  |  |  |
| Design and use two-way tables for discrete and grouped data                     |  |  |  |  |
| Use information provided to complete a two way table                            |  |  |  |  |

| Module 7: Displaying Data                                                                                                                                                                                                                                                                     | Notes | 😊 | 😐 | 😞 |
|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------|---|---|---|
| Produce: composite bar charts, comparative and dual bar charts, pie charts, histograms with equal or unequal class intervals and frequency diagrams for grouped discrete data, scatter graphs, line graphs, frequency polygons for grouped data, grouped frequency tables for continuous data |       |   |   |   |
| Interpret: composite bar charts, comparative and dual bar charts, pie charts, scatter graphs, frequency polygons and histograms                                                                                                                                                               |       |   |   |   |
| Recognise simple patterns, characteristics and relationships in line graphs and frequency polygons                                                                                                                                                                                            |       |   |   |   |
| Find the median from a histogram or any other information from a histogram, such as the number of people in a given interval                                                                                                                                                                  |       |   |   |   |

|                                                                                                                                                                          |  |  |  |  |
|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------|--|--|--|--|
| From line graphs, frequency polygons and frequency diagrams: read off frequency values, calculate total population, find greatest and least values                       |  |  |  |  |
| From pie charts: find the total frequency and find the frequency represented by each sector                                                                              |  |  |  |  |
| From histograms: complete a grouped frequency table and understand and define frequency density                                                                          |  |  |  |  |
| Present findings from databases, tables and charts                                                                                                                       |  |  |  |  |
| Look at data to find patterns and exceptions, explain an isolated point on a scatter graph                                                                               |  |  |  |  |
| Draw lines of best fit by eye, understanding what these represent                                                                                                        |  |  |  |  |
| Use a line of best fit, or otherwise, to predict values of one variable given values of the other variable                                                               |  |  |  |  |
| Distinguish between positive, negative and zero correlation using lines of best fit                                                                                      |  |  |  |  |
| Understand that correlation does not imply causality                                                                                                                     |  |  |  |  |
| Appreciate that correlation is a measure of the strength of the association between two variables and that zero correlation does not necessarily imply 'no relationship' |  |  |  |  |

END OF TERM: Test 2

# Term 2 Objectives

| Module 8: Construction & Loci                                                                                                                                                                                                                                             | Notes | 😊 | 😐 | 😞 |
|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------|---|---|---|
| Use straight edge and a pair of compasses to do standard constructions                                                                                                                                                                                                    |       |   |   |   |
| Construct triangles including an equilateral triangle                                                                                                                                                                                                                     |       |   |   |   |
| Understand, from the experience of constructing them, that triangles satisfying SSS, SAS, ASA and RHS are unique, but SSA triangles are not                                                                                                                               |       |   |   |   |
| Construct the perpendicular bisector of a given line                                                                                                                                                                                                                      |       |   |   |   |
| Construct the perpendicular from a point to a line                                                                                                                                                                                                                        |       |   |   |   |
| Construct the bisector of a given angle                                                                                                                                                                                                                                   |       |   |   |   |
| Construct angles of $60^\circ$ , $90^\circ$ , $30^\circ$ , $45^\circ$                                                                                                                                                                                                     |       |   |   |   |
| Construct a regular hexagon inside a circle                                                                                                                                                                                                                               |       |   |   |   |
| Construct diagrams of everyday 2-D situations involving rectangles, triangles, perpendicular and parallel lines                                                                                                                                                           |       |   |   |   |
| Draw and construct diagrams from given information                                                                                                                                                                                                                        |       |   |   |   |
| Construct: a region bounded by a circle and an intersecting line<br><br>– a given distance from a point and a given distance from a line<br><br>– equal distances from 2 points or 2 line segments<br><br>– regions which may be defined by 'nearer to' or 'greater than' |       |   |   |   |
| Find and describe regions satisfying a combination of loci                                                                                                                                                                                                                |       |   |   |   |

| Module 9: Types of Number                                                                                                                                                          | Notes | 😊 | 😐 | 😞 |
|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------|---|---|---|
| Identify factors, multiples and prime numbers                                                                                                                                      |       |   |   |   |
| Find the prime factor decomposition of positive integers                                                                                                                           |       |   |   |   |
| Find the common factors and common multiples of two numbers                                                                                                                        |       |   |   |   |
| Find the Highest Common Factor (HCF) and the Lowest Common Multiple (LCM) of two numbers                                                                                           |       |   |   |   |
| Recall integer squares from $2 \times 2$ to $15 \times 15$ and the corresponding square roots                                                                                      |       |   |   |   |
| Recall the cubes of 2, 3, 4, 5 and 10 and cube roots                                                                                                                               |       |   |   |   |
| Use index notation for squares and cubes                                                                                                                                           |       |   |   |   |
| Use index notation for integer powers of 10                                                                                                                                        |       |   |   |   |
| Use standard form, expressed in conventional notation                                                                                                                              |       |   |   |   |
| Be able to write very large and very small numbers presented in a context in standard form                                                                                         |       |   |   |   |
| Convert between ordinary and standard form representations                                                                                                                         |       |   |   |   |
| Interpret a calculator display using standard form                                                                                                                                 |       |   |   |   |
| Calculate with standard form                                                                                                                                                       |       |   |   |   |
| Use index laws to simplify and calculate the value of numerical expressions involving multiplication and division of integer negative and fractional powers, and powers of a power |       |   |   |   |

| Module 10: Patterns & Sequences                                                            | Notes | 😊 | 😐 | 😞 |
|--------------------------------------------------------------------------------------------|-------|---|---|---|
| Recognise sequences of odd and even numbers                                                |       |   |   |   |
| Generate simple sequences of numbers, squared integers and sequences derived from diagrams |       |   |   |   |
| Describe the term-to-term definition of a sequence in words                                |       |   |   |   |
| Identify which terms cannot be in a sequence                                               |       |   |   |   |
| Generate specific terms in a sequence using the position-to-term and term-to-term rules    |       |   |   |   |
| Find the $n$ th term of an arithmetic sequence                                             |       |   |   |   |
| Use the $n$ th term of an arithmetic sequence                                              |       |   |   |   |

| Module 11: 2D & 3D Shapes                                                                   | Notes | 😊 | 😐 | 😞 |
|---------------------------------------------------------------------------------------------|-------|---|---|---|
| Use 2-D representations of 3-D shapes                                                       |       |   |   |   |
| Use isometric grids                                                                         |       |   |   |   |
| Draw nets and show how they fold to make a 3-D solid                                        |       |   |   |   |
| Understand and draw front and side elevations and plans of shapes made from simple solids   |       |   |   |   |
| Given the front and side elevations and the plan of a solid, draw a sketch of the 3-D solid |       |   |   |   |

END OF HALF TERM: Test 3

| Module 12: Perimeter & Area                                                                                       | Notes | 😊 | 😐 | 😞 |
|-------------------------------------------------------------------------------------------------------------------|-------|---|---|---|
| Recall and use the formulae for the area of a triangle, rectangle and a parallelogram                             |       |   |   |   |
| Find the area of a trapezium                                                                                      |       |   |   |   |
| Calculate perimeter and area of compound shapes made from triangles, rectangles and other shapes                  |       |   |   |   |
| Find the surface area of simple shapes (prisms) using the formulae for triangles and rectangles, and other shapes |       |   |   |   |
| Find circumferences of circles and areas enclosed by circles                                                      |       |   |   |   |
| Recall and use the formulae for the circumference of a circle and the area enclosed by a circle                   |       |   |   |   |
| Use $\pi \approx 3.142$ or use the $\pi$ button on a calculator                                                   |       |   |   |   |
| Give an exact answer to a question involving the area or a circumference of a circle                              |       |   |   |   |
| Find the perimeters and areas of semicircles and quarter circles                                                  |       |   |   |   |
| Calculate the lengths of arcs and the areas of sectors of circles                                                 |       |   |   |   |
| Find the surface area of a cylinder                                                                               |       |   |   |   |
| Find the area of a segment of a circle given the radius and length of the chord                                   |       |   |   |   |
| Convert between metric units of area                                                                              |       |   |   |   |

| Module 13: Fractions, Decimals & Percentages                                                                                | Notes | 😊 | 😐 | 😞 |
|-----------------------------------------------------------------------------------------------------------------------------|-------|---|---|---|
| Understand that a percentage is a fraction in hundredths                                                                    |       |   |   |   |
| Convert between fractions, decimals and percentages                                                                         |       |   |   |   |
| Convert between recurring decimals and exact fractions and use proof                                                        |       |   |   |   |
| Write one number as a percentage of another number                                                                          |       |   |   |   |
| Calculate the percentage of a given amount                                                                                  |       |   |   |   |
| Find a percentage increase/decrease of an amount                                                                            |       |   |   |   |
| Reverse percentage, eg find the original cost of an item given the cost after a 10% deduction                               |       |   |   |   |
| Use a multiplier to increase by a given percentage over a given time , eg $1.18 \times 64$ increases 64 by 10% over 8 years |       |   |   |   |
| Calculate simple and compound interest                                                                                      |       |   |   |   |

END OF TERM: Test 4

## Term 3 Objectives

| Module 14: Formulae & Linear Equations                                                                                                              | Notes | 😊 | 😐 | 😞 |
|-----------------------------------------------------------------------------------------------------------------------------------------------------|-------|---|---|---|
| Derive a formula                                                                                                                                    |       |   |   |   |
| Use formulae from mathematics and other subjects                                                                                                    |       |   |   |   |
| Substitute numbers into a formula                                                                                                                   |       |   |   |   |
| Substitute positive and negative numbers into expressions such as $3x^2 + 4$ and $2x^3$                                                             |       |   |   |   |
| Set up linear equations from word problems                                                                                                          |       |   |   |   |
| Solve simple linear equations                                                                                                                       |       |   |   |   |
| Solve linear equations, with integer coefficients, in which the unknown appears on either side or on both sides of the equation                     |       |   |   |   |
| Solve linear equations that include brackets, those that have negative signs occurring anywhere in the equation, and those with a negative solution |       |   |   |   |
| Solve linear equations in one unknown, with integer or fractional coefficients                                                                      |       |   |   |   |
| Solve simple linear inequalities in one variable, and represent the solution set on a number line                                                   |       |   |   |   |
| Use the correct notation to show inclusive and exclusive inequalities                                                                               |       |   |   |   |
| Change the subject of a formula including cases where the subject is on both sides of the original formula, or where a power of the subject appears |       |   |   |   |

| Module 15: Linear Graphs                                                                                                                                                                                           | Notes | 😊 | 😐 | 😞 |
|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------|---|---|---|
| Recognise that equations of the form $y = mx + c$ correspond to straight-line graphs in the coordinate plane                                                                                                       |       |   |   |   |
| Draw and interpret straight line graphs for real-life situations<br>– ready reckoner graphs<br>– conversion graphs<br>– fuel bills, eg gas and electric<br>– fixed charge (standing charge) and cost per unit      |       |   |   |   |
| Plot and draw graphs of straight lines with equations of the form $y = mx + c$                                                                                                                                     |       |   |   |   |
| Find the gradient of a straight line from a graph                                                                                                                                                                  |       |   |   |   |
| Analyse problems and use gradients to interpret how one variable changes in relation to another                                                                                                                    |       |   |   |   |
| Interpret and analyse a straight-line graph                                                                                                                                                                        |       |   |   |   |
| Understand that the form $y = mx + c$ represents a straight line                                                                                                                                                   |       |   |   |   |
| Find the gradient of a straight line from its equation                                                                                                                                                             |       |   |   |   |
| Explore the gradients of parallel lines and lines perpendicular to each other                                                                                                                                      |       |   |   |   |
| Write down the equation of a line parallel or perpendicular to a given line                                                                                                                                        |       |   |   |   |
| Use the fact that when $y = mx + c$ is the equation of a straight line then the gradient of a line parallel to it will have a gradient of $m$ and a line perpendicular to this line will have a gradient of $-1/m$ |       |   |   |   |
| Interpret and analyse a straight line graph and generate equations of lines parallel and perpendicular to the given line                                                                                           |       |   |   |   |
| Show the solution set of several inequalities in two variables on a graph                                                                                                                                          |       |   |   |   |

| Module 16: Simultaneous Equations                                                                                      | Notes | 😊 | 😐 | 😞 |
|------------------------------------------------------------------------------------------------------------------------|-------|---|---|---|
| Find the exact solutions of two simultaneous equations in two unknowns                                                 |       |   |   |   |
| Use elimination or substitution to solve simultaneous equations                                                        |       |   |   |   |
| Interpret a pair of simultaneous equations as a pair of straight lines and their solution as the point of intersection |       |   |   |   |
| Set up and solve a pair of simultaneous equations in two variables                                                     |       |   |   |   |

| Module 17: Probability                                                                                               | Notes | 😊 | 😐 | 😞 |
|----------------------------------------------------------------------------------------------------------------------|-------|---|---|---|
| Write probabilities using fractions, percentages or decimals                                                         |       |   |   |   |
| Understand and use estimates or measures of probability, including relative frequency                                |       |   |   |   |
| Use theoretical models to include outcomes using dice, spinners, coins etc                                           |       |   |   |   |
| Find the probability of successive events, such as several throws of a single dice                                   |       |   |   |   |
| Estimate the number of times an event will occur, given the probability and the number of trials                     |       |   |   |   |
| List all outcomes for single events, and for two successive events, systematically                                   |       |   |   |   |
| Use and draw sample space diagrams                                                                                   |       |   |   |   |
| Add simple probabilities, eg from sample space diagrams                                                              |       |   |   |   |
| Identify different mutually exclusive outcomes and know that the sum of the probabilities of all these outcomes is 1 |       |   |   |   |
| Use $1 - p$ as the probability of an event not occurring where $p$ is the probability of the event occurring         |       |   |   |   |

|                                                              |  |  |  |  |
|--------------------------------------------------------------|--|--|--|--|
| Find a missing probability from a list or table              |  |  |  |  |
| Understand conditional probabilities                         |  |  |  |  |
| Understand selection with or without replacement             |  |  |  |  |
| Draw a probability tree diagram based on given information   |  |  |  |  |
| Use a tree diagram to calculate conditional probability      |  |  |  |  |
| Compare experimental data and theoretical probabilities      |  |  |  |  |
| Compare relative frequencies from samples of different sizes |  |  |  |  |

END OF YEAR: Test 5

| Module 18: Ratio & Scale                                                                                                                                                                | Notes | 😊 | 😐 | 😞 |
|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------|---|---|---|
| Use ratios                                                                                                                                                                              |       |   |   |   |
| Write ratios in their simplest form                                                                                                                                                     |       |   |   |   |
| Divide a quantity in a given ratio                                                                                                                                                      |       |   |   |   |
| Solve a ratio problem in a context                                                                                                                                                      |       |   |   |   |
| Use and interpret maps and scale drawings                                                                                                                                               |       |   |   |   |
| Read and construct scale drawings drawing lines and shapes to scale                                                                                                                     |       |   |   |   |
| Estimate lengths using a scale diagram                                                                                                                                                  |       |   |   |   |
| Solve word problems about ratio and proportion                                                                                                                                          |       |   |   |   |
| Calculate an unknown quantity from quantities that vary in direct or inverse proportion                                                                                                 |       |   |   |   |
| Set up and use equations to solve word and other problems involving direct proportion or inverse proportion and relate algebraic solutions to graphical representation of the equations |       |   |   |   |

| Module 19: Averages & Range                                                                                                                     | Notes | 😊 | 😐 | 😞 |
|-------------------------------------------------------------------------------------------------------------------------------------------------|-------|---|---|---|
| Calculate mean, mode, median and range for small data sets                                                                                      |       |   |   |   |
| Recognise the advantages and disadvantages between measures of average                                                                          |       |   |   |   |
| Produce ordered stem and leaf diagrams and use them to find the range and averages                                                              |       |   |   |   |
| Calculate averages and range from frequency tables (Use $\Sigma x$ and $\Sigma fx$ )                                                            |       |   |   |   |
| Estimate the mean for large data sets with grouped data (and understand that it is an estimate)                                                 |       |   |   |   |
| Draw and interpret cumulative frequency tables and graphs                                                                                       |       |   |   |   |
| Use cumulative frequency graphs to find median, quartiles and interquartile range                                                               |       |   |   |   |
| Draw box plots from a cumulative frequency graph                                                                                                |       |   |   |   |
| Compare the measures of spread between a pair of box plots/cumulative frequency graphs                                                          |       |   |   |   |
| Interpret box plots to find median, quartiles, range and interquartile range                                                                    |       |   |   |   |
| Find the median from a histogram                                                                                                                |       |   |   |   |
| Compare distributions and make inferences, using the shapes of distributions and measures of average and spread, including median and quartiles |       |   |   |   |
| Find quartile and interquartile range from data                                                                                                 |       |   |   |   |
| Find modal class and interval containing the median                                                                                             |       |   |   |   |

END OF YEAR 10 WORK